

# Reaction mechanisms of phosphorus fluorides: An ab initio study <sup>1</sup>

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## Abstract

Reaction mechanisms of phosphorus fluorides may be analyzed on the basis of the coordination model of reaction mechanisms. Some of the intermediates and mechanistic details arising out of such an analysis have been investigated by ab initio molecular orbital calculations. The rapid equilibrium between five- and six-coordinate phosphorus fluorides, and exchange of axial and equatorial fluorines in PF<sub>5</sub>, is investigated by calculating the structures of adducts of phosphorus pentafluoride, i.e. D–PF<sub>5</sub> where D = NH<sub>3</sub>, H<sub>2</sub>O, CH<sub>3</sub>F, HF, PF<sub>3</sub> and PF<sub>6</sub><sup>–</sup>. Bond cleavage in phosphorus fluorides is investigated by calculating the structure of a fluorine-bridged anion P<sub>2</sub>F<sub>11</sub><sup>–</sup>. A reaction pathway is proposed for the fluoride-catalyzed oxidation of phosphorus(III) to phosphorus(V) fluorides which involves the known species PF<sub>3</sub>, PF<sub>4</sub><sup>–</sup> and PF<sub>5</sub>. © Elsevier Science S.A.

**Keywords:** Phosphorus fluorides; Reaction mechanisms; Ab initio calculations

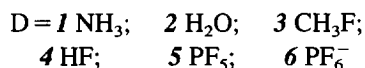
## 1. Introduction

Reaction mechanisms may be analyzed on the basis of the coordination model of reaction mechanisms [1]. This model emphasizes the discrete variables of coordination number and electron count, as well as the connectivity of atoms along a reaction pathway, and classifies the elementary steps of reactions as +C, –C, +C<sup>c</sup>, –C<sup>c</sup>. Reaction pathways may be tested by ab initio molecular orbital calculations, e.g. the mechanism of cleavage of Si–F and Si–C bonds in fluorosilicates [2], or oxidative fluorination of sulfur(IV) to sulfur(VI) compounds [3]. Other reaction pathways have been tested by kinetic simulation, e.g. the BF<sub>3</sub>–base system [4]. Calculations have now been carried out for phosphorus fluorides, and these results are related to mechanistic details such as rapid equilibria between five- and six-coordinate phosphorus compounds, exchange of axial and equatorial fluorines in PF<sub>5</sub>, the cleavage of P–F bonds in phosphorus compounds, and the mechanism of oxidation of phosphorus(III) to phosphorus(V) fluorides.

## 2. Results and discussion

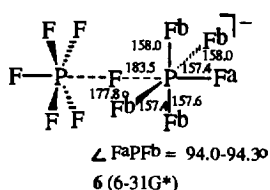
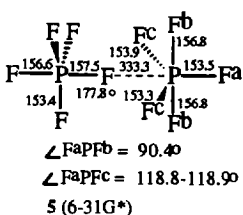
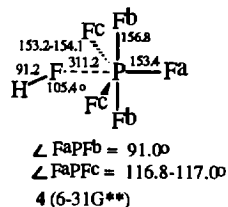
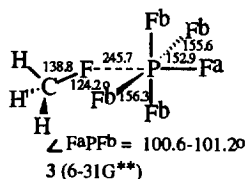
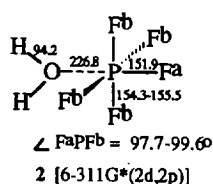
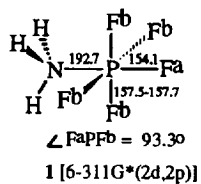
In order to test the statement that trigonal bipyramidal molecules are among the most sensitive indicators of bond

formation, +C, because of the change in symmetry and NMR spin pattern that accompanies the formation of six-coordinate adducts or intermediates [1], we studied the interaction of PF<sub>5</sub> with Lewis bases of widely differing basicity (Eq. (1)), and calculated the structures of adducts 1–6.



As a six-coordinate adduct such as H<sub>3</sub>N–PF<sub>5</sub> 1 is formed, the coordination number of phosphorus is increased from 5 to 6, and nitrogen from 3 to 4, i.e. +C<sub>P(5)N(3)</sub>. Cleavage of a P–N bond in adduct 1 is denoted as –C<sub>P(5)N(3)</sub>. If the calculated structures confirm that four basal fluorines in adducts 1–6 are essentially equivalent, then it is reasonable to assume that an equilibrium between five- and six-coordinate phosphorus species (Eq. (1)), can provide a pathway for the exchange of axial and equatorial fluorines in PF<sub>5</sub>. Our criterion for evaluating the equivalence of four basal P–F<sup>b</sup> bonds is based on a qualitative comparison of P–F<sup>b</sup> bond lengths and ∠F<sup>a</sup>PF<sup>b</sup> bond angles. Other means of estimating the distortion from D<sub>3h</sub> or C<sub>4v</sub> symmetry in phosphorus or silicon fluorides have been proposed by Holmes [5].

<sup>1</sup> Dedicated to Professor Alois Haas on the occasion of his 65th birthday.



Of adducts 1–6, only 1 is sufficiently inert to allow characterization by NMR and X-ray crystallography [6], but there is some indirect support for the existence of 2–6. For example, adduct 2 has not been characterized, but the closely related adduct  $\text{Et}_2\text{O}-\text{F}_5$  is stable below  $-65^\circ\text{C}$  [7]. Furthermore, the deprotonated anion  $\text{F}_3\text{PO}^{2-}$  [8], and related species  $\text{F}_3\text{AsOH}^-$  [9] and  $\text{H}_2\text{O}-\text{GeF}_5^-$  [10], have been described in the literature. The adducts  $\text{H}_3\text{N}-\text{F}_5$  1 and  $\text{H}_2\text{O}-\text{PF}_5$  2 are reasonable intermediates of ammonolysis and hydrolysis reactions, respectively [6,7]. Adducts  $\text{CH}_3\text{F}-\text{PF}_5$  3 and  $\text{HF}-\text{PF}_5$  4 are unknown, but related adducts with somewhat stronger Lewis acids have been identified by NMR at low temperature, e.g.  $\text{CH}_3\text{F}-\text{AsF}_5$  and  $\text{CH}_3\text{F}-\text{SbF}_5$  [11]. Suggestions have been made that dimeric  $\text{PF}_5$  5 [12], or dimeric  $\text{SiF}_5^-$  [13], might contribute to axial–equatorial ligand exchange. NMR studies on the  $\text{PF}_5-\text{PF}_6^-$  [14] and  $\text{PhPF}_4-\text{PhPF}_5^-$  [15] systems confirm that rapid P–F bond cleavage occurs in these systems, and a bridged intermediate, e.g.  $\text{P}_2\text{F}_{11}^-$  6, can account for the NMR results.

Calculations were carried out with several basis sets and they confirm that four basal fluorines in adduct  $\text{H}_3\text{N}-\text{PF}_5$  1 are essentially equivalent. With the 6-311G\* (2d,2p) basis set, the four basal P–F<sup>b</sup> bond lengths in 1 are in the range 157.5–157.7 pm, and the four angles between the apical and basal fluorines,  $\angle\text{F}^a\text{PF}^b$ , are all  $93.3^\circ$ . With the 3-21G\* basis set, very similar results were obtained, namely, four basal P–F<sup>b</sup> bond lengths in the range 158.1–158.2 pm, and four angles  $\angle\text{F}^a\text{PF}^b$  in the range  $94.5$ – $94.6^\circ$ . Calculations therefore show that all basal P–F<sup>b</sup> bonds in adduct 1 are essentially equivalent. These results may be compared with experimental P–F<sup>b</sup> bond lengths in the solid state, which are in the range 158.9–160.0 pm, and  $\angle\text{F}^a\text{PF}^b$  in the range  $90.8$ – $92.3^\circ$  [6].

The calculated lengths of the P–N bond in 1 are 192.7 pm [6-311G\* (2d,2p)], 193.1 pm (3-21G\*), and 195.1 pm (MINI-1). In the solid state, the experimental P–N bond length is 184.2 pm [6].

Calculations with the 6-311G\* (2d,2p) basis set also show that adduct  $\text{H}_2\text{O}-\text{PF}_5$  2 has four essentially equivalent basal fluorines, with P–F<sup>b</sup> bond lengths in the range 154.3–155.5 pm, and bond angles  $\angle\text{F}^a\text{PF}^b$  in the range  $97.7$ – $99.6^\circ$ . It was suggested some time ago that the rapid formation and dissociation of adduct 2 can lead to exchange of axial and equatorial fluorines in  $\text{PF}_5$  [7].

Adduct  $\text{CH}_3\text{F}-\text{PF}_5$  3 was selected to test the hypothesis that ‘‘inert’’ solvents may bring about axial–equatorial ligand exchange in  $\text{PF}_5$  without participating in further chemical reactions [1]. Calculations with the 6-31G\* basis set show four basal P–F<sup>b</sup> bond lengths in the range 155.6–156.3 pm, and  $\angle\text{F}^a\text{PF}^b$  in the range  $100.6$ – $101.2^\circ$ . These results strongly imply that axial and equatorial fluorines in  $\text{PF}_5$  can be exchanged as a result of interaction with a solvent such as  $\text{CH}_3\text{F}$ . A similar conclusion is reached on the basis of 3-21G\* calculations, which show four basal P–F<sup>b</sup> bond lengths in the range 155.9–157.4 pm, and four bond angles  $\angle\text{F}^a\text{PF}^b$  in the range  $97.0$ – $98.0^\circ$ .

It is uncertain from our calculation of 4 or 5 whether interaction with HF, or with another  $\text{PF}_5$  molecule, leads to exchange of axial and equatorial fluorines in  $\text{PF}_5$ . Adduct 4 (6-31G\*\*) shows a relatively large variation in P–F<sup>b</sup> and P–F<sup>c</sup> bond lengths in the range of 153.2–156.8 pm, and bond angles  $\angle\text{F}^a\text{PF}^b$  and  $\angle\text{F}^a\text{PF}^c$  in the range  $91.0$ – $117.0^\circ$ . The long bond between HF and  $\text{PF}_5$ , namely, 311.2 pm (6-31G\*\*), or 211.1 pm (3-21G\*), implies that 4 is a very weakly bound adduct in which the  $\text{PF}_5$  moiety is only slightly distorted. Similar comments can be made about the  $\text{PF}_5$  dimer 5, where calculation (6-31G\*) shows relatively large variation in basal P–F bond lengths 153.3–156.8 pm, and  $\angle\text{F}^a\text{PF}^b$  and  $\angle\text{F}^a\text{PF}^c$  bond angles,  $90.4$ – $118.9^\circ$ .

Calculation (6-31G\*) of the fluorine-bridged anion  $\text{P}_2\text{F}_{11}^-$  6 shows four basal P–F<sup>b</sup> bond lengths in the range 157.4–158.0 pm, and  $\angle\text{F}^a\text{PF}^b$  in the range  $94.0$ – $94.3^\circ$ , indicating that 6 has essentially equivalent basal fluorines.

In summary, the calculations described above are in agreement with the view that axial and equatorial fluorines in  $\text{PF}_5$  undergo intramolecular ligand exchange as a result of bond formation, +C, whenever  $\text{PF}_5$  interacts with a donor molecule such as  $\text{NH}_3$ ,  $\text{OH}_2$ ,  $\text{CH}_3\text{F}$  and  $\text{PF}_6^-$ , to give adducts 1–3,6 (Eq. (1)). The calculated structures of adducts 4–5, however, suggest that interaction with HF, or with another  $\text{PF}_5$  molecule, probably does not bring about exchange of axial and equatorial fluorines in  $\text{PF}_5$ .

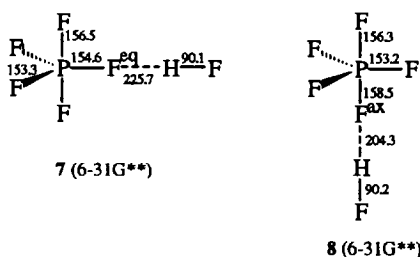
Turning to the question of bond cleavage, –C, in phosphorus fluorides, NMR studies show clearly that rapid bond cleavage occurs in the  $\text{PF}_5-\text{PF}_6^-$  [14] and  $\text{PhPF}_4-\text{PhPF}_5^-$  [15] systems. The calculated structure of intermediate 6 shows a substantially longer/weaker P···F bridging bond of 183.5 pm, as compared to the terminal P–F bond lengths of 157.4–158.0 pm. This calculated (6-31G\*) bridge bond of

183.5 pm may be compared with a previous calculation of 183.1 pm [16]. An analogously bridged intermediate  $\text{Si}_2\text{F}_{11}^{3-}$  can account for rapid intermolecular fluorine exchange in the  $\text{SiF}_5^-$ – $\text{SiF}_6^{2-}$  system [13]. As the strength of the bridging bond increases in related anions such as  $\text{As}_2\text{F}_{11}^-$  or  $\text{Sb}_2\text{F}_{11}^-$ , the bridged species can be identified in solution, or isolated [17].

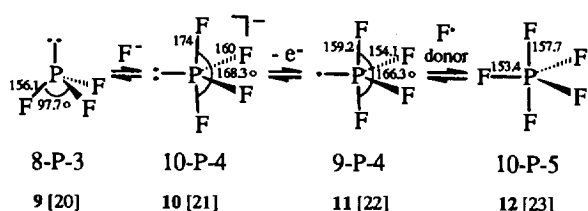
NMR experiments show that P–F coupling is retained in purified samples of  $\text{PF}_5$ , or when  $\text{PF}_5$  is dissolved in solvents such as  $\text{CH}_3\text{F}$  [1]. Furthermore,  $\text{PF}_5$  is a nonelectrolyte and has a small solubility in hydrogen fluoride [18]. Based on the calculated structures of **3–5**, only cleavage of the weakest/longest P–F bridge bond in **3–5** is expected, which leaves the original  $\text{PF}_5$  molecule intact. For example, the calculated long/weak bridging P–F bond in **3**, namely, 245.7 pm (6-31G\*) or 196.5 (3-21G\*), may be compared to the shorter/stronger terminal P–F bonds of 152.9–156.3 pm (6-31G\*), or 154.1–157.4 pm (3-21G\*). Only a simple dissociation of adduct  $\text{CH}_3\text{F}$ – $\text{PF}_5$  **3** is thus expected, with no further chemical reaction, and this result is consistent with the known stability of  $\text{PF}_5$  in hydrocarbon and halogenated solvents.

Similar arguments can be applied to **4** and **5** to account for the chemical stability of  $\text{PF}_5$  in the presence of HF, or in the presence of other  $\text{PF}_5$  molecules.

To test for the possibility that hydrogen bonding might lead to P–F bond cleavage, the calculation (6-31G\*\*) of **7** and **8** was carried out. Other than a small lengthening of the axial or equatorial P–F bond, however, no significant changes are evident in the  $\text{PF}_5$  moiety. The trigonal bipyramidal geometry of  $\text{PF}_5$  is not significantly distorted, therefore, neither chemical reaction nor axial–equatorial fluorine exchange is expected as a result of the formation of hydrogen-bridged intermediates **7–8**.



Finally, a mechanism of oxidation of phosphorus(III) to phosphorus(V) fluorides is proposed (Scheme 1) which is based on the mechanism of oxidation of sulfur(IV) to sulfur(VI) fluorides in the presence of fluoride ion [3]. The latter mechanism postulates initial attack of  $\text{F}^-$  on sulfur(IV)



Scheme 1. Proposed mechanism of oxidation of P(III) to P(V) fluorides in the presence of  $\text{F}^-$ .

compounds, followed by oxidation to a fluorosulfur radical and, lastly, reaction with a suitable fluorine atom donor to give the sulfur(VI) product. The  $N$ – $X$ – $L$  notation of Perkins et al. [19] is used in Scheme 1 to specify the valence electron count ( $N$ ) and coordination number ( $L$ ) of phosphorus ( $X$ ). Calculations for **9–12** were not carried out in this study because both calculated and experimental results have been reported by others [20–23].

The fact that  $\text{F}^-$  adds readily to  $\text{PF}_3$  to give anion  $\text{PF}_4^-$ , in solution [21] or in the gas phase [24], is in agreement with the first step of the proposed mechanism (Scheme 1). In the absence of  $\text{F}^-$  (and  $\text{PF}_4^-$ ), the mechanism of oxidation is presumably simplified to  $\text{PF}_3 \rightarrow \text{PF}_4^\cdot \rightarrow \text{PF}_5$ , as suggested for the free-radical addition of fluorine atoms to  $\text{PF}_3$  [25]. In principle, there is a sharp distinction between an oxidation that occurs in the presence of  $\text{F}^-$ , and a free-radical oxidation that occurs in the absence of  $\text{F}^-$ , but this distinction may be difficult to observe in practice because of the inadvertent introduction of fluoride ion during the course of typical oxidative fluorinations. The finding that the rate of oxidative chlorination of  $\text{PF}_3$  is photosensitive, but also catalyzed by glass surfaces [26], hints at experimental difficulties.

Scheme 1 does not identify the electron acceptor that converts anion  $\text{PF}_4^-$  **10** to radical  $\text{PF}_4^\cdot$  **11**. However, for the related anion-to-radical oxidation of  $\text{PhSiF}_5^{2-}$  to  $\text{PhSiF}_5^\cdot$ , numerous one-electron acceptors can be used, including metal ions, halogen compounds, tetracyanoethylene, etc. [27].

The last step of Scheme 1 involves the interaction of  $\text{PF}_4^\cdot$  with a fluorine atom donor to give the product  $\text{PF}_5$ . For typical oxidative fluorinating agents such as  $\text{F}_2$ ,  $\text{ClF}$  or  $\text{XeF}_2$ , we postulate that rapid bond cleavage occurs as a result of the formation of intermediates  $\text{F}_4\text{P}^\cdot\text{F}\cdots\text{F}\cdot$ ,  $\text{F}_4\text{P}^\cdot\text{F}\cdots\text{Cl}\cdot$  or  $\text{F}_4\text{P}^\cdot\text{F}\cdots\text{XeF}\cdot$ , respectively. An explanation for the catalytic role of  $\text{F}^-$  is then apparent, because the presence of  $\text{F}^-$  allows bond cleavage of very weakly bound intermediates, e.g.,  $\text{F}_4\text{P}^\cdot\text{F}\cdots\text{F}\cdot \rightarrow \text{PF}_5 + \text{F}\cdot$ , however, in the absence of  $\text{F}^-$  the oxidizing agents themselves must undergo bond cleavage to give radical intermediates, e.g.  $\text{F}^\cdot\text{F} \rightarrow 2\text{F}\cdot$ .

It is interesting to speculate whether the catalytic role of  $\text{F}^-$  (Scheme 1) applies to less electronegative anions such as  $\text{Cl}^-$ , and the  $X$ -ray structure of anion  $\text{PCl}_4^-$  provides some insight into this question. There are nonequivalent axial P–Cl bonds in  $\text{PCl}_4^-$ , 211.8 and 285.0 pm [28], and the substantial lengthening of one of the axial P–Cl bonds (285.0 pm) raises the possibility that the lifetime of anion  $\text{PCl}_4^-$  in solution might be relatively short, as compared to that of anion  $\text{PF}_4^-$ . This suggests that electronegative anions such as  $\text{F}^-$ , and perhaps  $\text{HO}^-$ , are suitable catalysts for oxidation of phosphorus(III) compounds, whereas larger and less electronegative anions such as  $\text{Cl}^-$  or  $\text{Br}^-$  are less effective. Without a catalyst, oxidation may follow a free-radical pathway and, indeed, radical  $\text{PCl}_4^\cdot$  is a known species [29].

### 3. Methods

The GAUSSIAN 92 system of programs [30] was used for all ab initio molecular orbital calculations. Interacting mole-

cules and ions were treated as one large system and were fully optimized with analytical gradient method at restricted Hartree–Fock level, using basis sets 3-21\* and 6-31G\*. Polarization basis sets, 6-31G\*\*, with p orbitals for each hydrogen, were used for hydrogen-bond structures **4**, **7** and **8**, and triple split-valence orbital basis set 6-31G\* (2d,2p) were used for structure **1** and **2**.

For the MINI-1 calculations, Huzinaga's minimal basis set [31] was used with the atomic scaling factors of Deisz [32]. Binding energies were determined by the supermolecule approach with the full counterpoise correction of Boys and Bernardi [33].

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### References

- [1] A.F. Janzen, *Coord. Chem. Rev.* 130 (1994) 355.
- [2] X. Ou, A.F. Janzen, *Inorg. Chem.*, in press.
- [3] (a) X. Ou, A.F. Janzen, *Can. J. Chem.*, in press; (b) A.F. Janzen, X. Ou, *J. Fluorine Chem.* 71 (1995) 207.
- [4] X. Ou, R. Wallace, A.F. Janzen, *Can. J. Chem.* 71 (1993) 51.
- [5] R.R. Holmes, *Chem. Rev.* 90 (1990) 17.
- [6] W. Storzer, D. Schomburg, G.-V. Rösenthaller, R. Schmutzler, *Chem. Ber.* 116 (1983) 367.
- [7] J.A. Gibson, D.G. Ibbott, A.F. Janzen, *Can. J. Chem.* 51 (1973) 3203.
- [8] M. Kant, M. Meisel, *Z. Anorg. Allg. Chem.* 620 (1994) 1937.
- [9] L. Kolditz, W. Röhsch, *Z. Anorg. Allg. Chem.* 293 (1957) 168.
- [10] I. Wharf, M. Onyszchuk, *Can. J. Chem.* 48 (1970) 2250.
- [11] J.-Y. Calves, R.J. Gillespie, *J. Am. Chem. Soc.* 99 (1977) 1788.
- [12] J.I. Musher, *Tetrahedron Lett.* (1973) 1093.
- [13] R.K. Marat, A.F. Janzen, *Can. J. Chem.* 55 (1977) 3845.
- [14] S. Brownstein, J. Bornais, *Can. J. Chem.* 46 (1968) 225.
- [15] C. Wang, A.F. Janzen, *Can. J. Chem.* 62 (1984) 1563.
- [16] C. Kölmel, G. Palm, R. Ahlrichs, M. Bär, A.I. Boldyrev, *Chem. Phys. Lett.* 173 (1990) 151.
- [17] (a) P.A.W. Dean, R.J. Gillespie, R. Hulme, D.A. Humphreys, *J. Chem. Soc. A* (1971) 341; (b) C.G. Davies, R.J. Gillespie, P.R. Ireland, J.M. Sowa, *Can. J. Chem.* 52 (1974) 2048.
- [18] (a) A.F. Clifford, S. Kongpricha, *J. Inorg. Nucl. Chem.* 20 (1961) 147; (b) R. Gut, K. Gantschi, *J. Inorg. Nucl. Chem. Suppl.* (1976) 95.
- [19] C.W. Perkins, J.C. Martin, A.J. Arduengo, W. Lau, A. Alegria, J.K. Kochi, *J. Am. Chem. Soc.* 102 (1980) 7753.
- [20] Y. Kawashima, A.P. Cox, *J. Mol. Spectrosc.* 65 (1977) 319.
- [21] K.O. Christe, D.A. Dixon, H.P.A. Mercier, J.C.P. Sanders, G.J. Schrobilgen, W.W. Wilson, *J. Am. Chem. Soc.* 116 (1994) 2850.
- [22] C.J. Cramer, M.H. Lim, *J. Phys. Chem.* 98 (1994) 5024.
- [23] K.W. Hansen, L.S. Bartell, *Inorg. Chem.* 4 (1965) 1775.
- [24] T.C. Rhyne, J.G. Dillard, *Inorg. Chem.* 10 (1971) 730.
- [25] I.B. Goldberg, H.R. Crowe, D. Pilipovich, *Chem. Phys. Lett.* 33 (1975) 347.
- [26] J.N. Wilson, *J. Am. Chem. Soc.* 80 (1958) 1338.
- [27] K. Tamao, J. Yoshida, H. Yamamoto, T. Kakui, H. Matsumoto, M. Takahashi, A. Kurita, M. Murata, M. Kumada, *Organometallics* 1 (1982) 355.
- [28] K.B. Dillon, A.W.G. Platt, A. Schmidpeter, F. Zwaschka, W.S. Sheldrick, *Z. Anorg. Allg. Chem.* 488 (1982) 7.
- [29] (a) G.L. Gutsev, *Chem. Phys.* 179 (1994) 325; (b) G.F. Kokoszka, F.E. Brinckman, *J. Am. Chem. Soc.* 92 (1970) 1199.
- [30] M.J. Frisch, G.W. Trucks, M. Head-Gordon, P.M.W. Gill, M.W. Wong, J.B. Foresman, B.G. Johnson, H.B. Schlegel, M.A. Robb, E.S. Replogle, R. Gomperts, J.L. Andres, K. Raghavachari, J.S. Binkley, C. Gonzalez, R.L. Martin, D.J. Fox, D.J. Defrees, J. Baker, J.J.P. Stewart, J.A. Pople, GAUSSIAN 92, Revision C, Gaussian, Pittsburgh, PA, 1992.
- [31] S. Huzinaga, J. Andzelm, M. Klobukowski, E. Radzio-Andzelm, Y. Sakai, H. Tatewaki, *Gaussian Basis Sets for Molecular Calculations*, Elsevier, Amsterdam, 1984.
- [32] M.W. Schmidt, J.A. Boatz, K.K. Baldrige, S. Koseki, M.S. Gordon, S.T. Elbert, B. Lam, *GAMESS, QCPE Bull.* 7 (1987) 115.
- [33] S.F. Boys, F. Bernardi, *Mol. Phys.* 19 (1970) 553.